

Carleton University

Investigation of Kronecker-based Recovery in Compressive Sensing¹

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Original signal, $\mathbf{x}_{N \times 1}$



Compressive Sensing (CS)

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$$\mathbf{y}_{M \times 1} = \Phi_{M \times N} \mathbf{x}_{N \times 1}$$



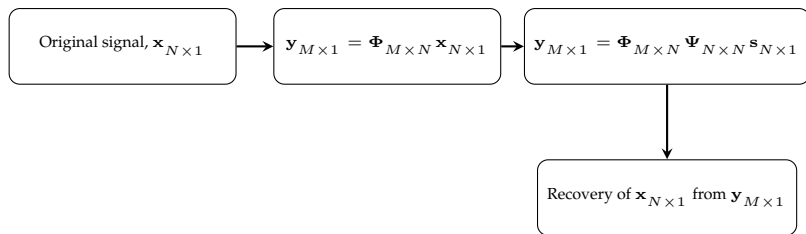
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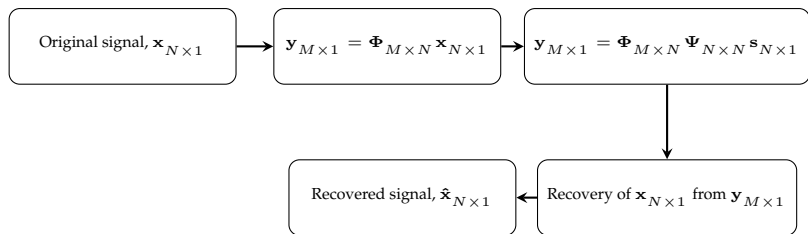


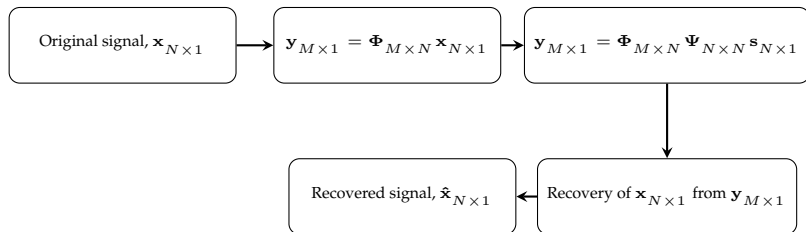
$$\mathbf{y}_{M \times 1} = \Phi_{M \times N} \mathbf{x}_{N \times 1}$$



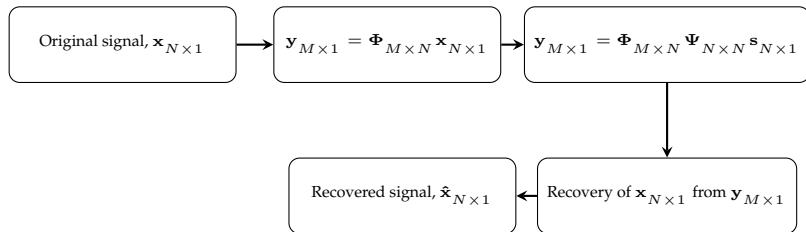
$$\mathbf{y}_{M \times 1} = \Phi_{M \times N} \Psi_{N \times N} \mathbf{s}_{N \times 1}$$





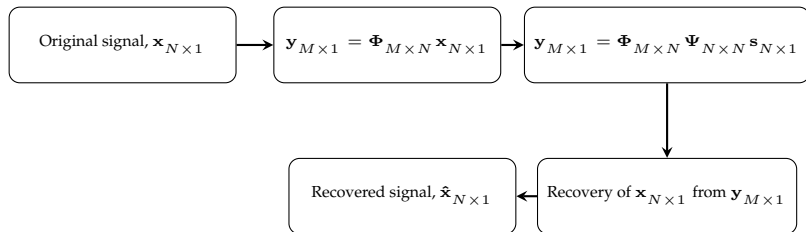


How to find the sparse solution to the linear system?



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✓ $\min \|\mathbf{s}\|_0$ subject to $\mathbf{y} = \Phi \Psi \mathbf{s} \rightarrow$ Non-convex optimization problem, **NP hard to solve.**



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- ✓ $\min \|\mathbf{s}\|_0$ subject to $\mathbf{y} = \Phi \Psi \mathbf{s} \rightarrow$ Non-convex optimization problem, **NP hard to solve**.
- ✓ $\min \|\mathbf{s}\|_1$ subject to $\mathbf{y} = \Phi \Psi \mathbf{s} \rightarrow$ **Solvable** convex optimization problem leading to same solution with ℓ_0 norm.

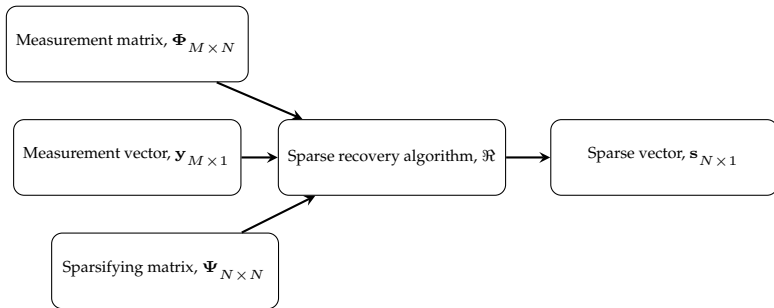


Figure: Block diagram representation of sparse reconstruction

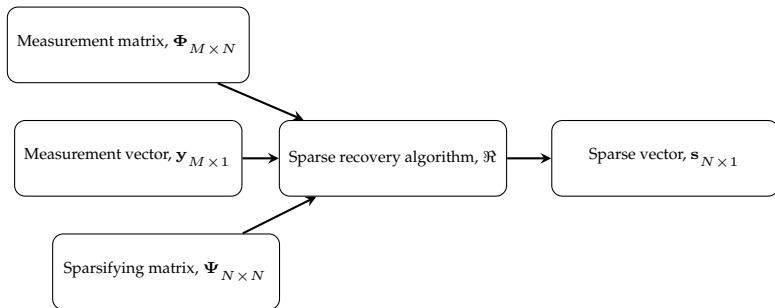


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$$\mathbf{s}_{N \times 1} = \mathfrak{R}(\mathbf{y}_{M \times 1}, \Phi_{M \times N}, \Psi_{N \times N})$$

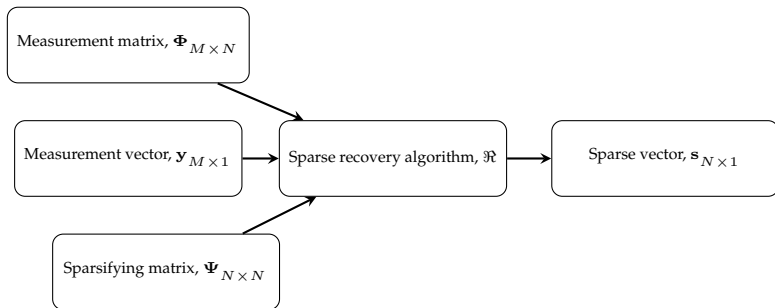


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What majorly determines the quality of the reconstructed signal?

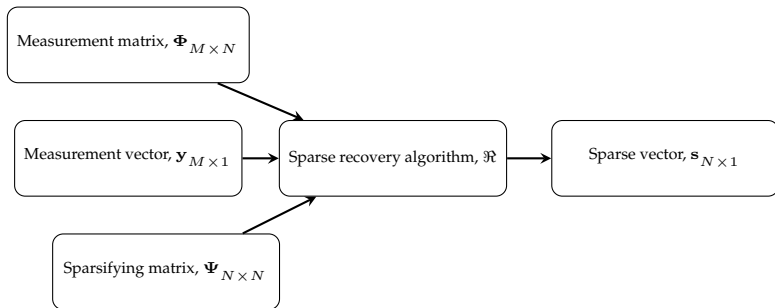


Figure: Block diagram representation of sparse reconstruction

$$\mathbf{s}_{N \times 1} = \mathfrak{R}(\mathbf{y}_{M \times 1}, \Phi_{M \times N}, \Psi_{N \times N})$$

What majorly determines the quality of the reconstructed signal?

- **Lower** the mutual coherence (μ) between Φ and Ψ , **better** the quality.

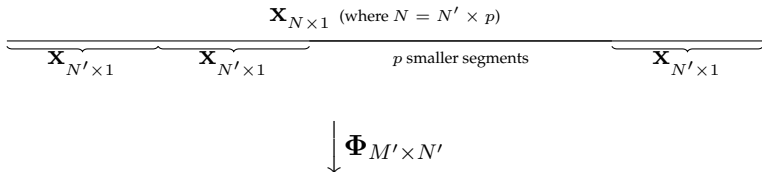


$\mathbf{x}_{N \times 1}$



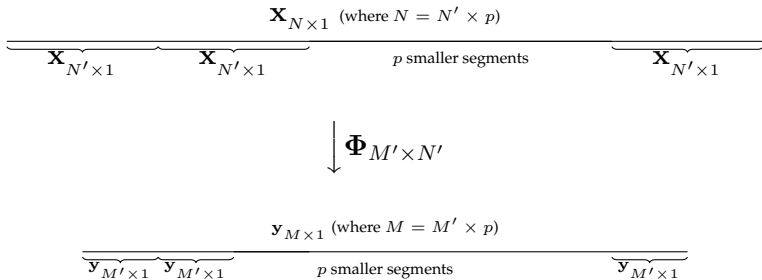
$$\underbrace{\mathbf{X}_{N' \times 1}} \quad \underbrace{\mathbf{X}_{N' \times 1}} \quad \underbrace{\hspace{10em}}_{p \text{ smaller segments}} \quad \underbrace{\mathbf{X}_{N' \times 1}}$$

$\mathbf{X}_{N \times 1}$ (where $N = N' \times p$)





Segmentation-based Sensing





Advantages:



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1. Generation of smaller Φ



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1. **Continuous bio-signal (e.g. ECG) monitoring** using 'resource constraint' wearable devices.



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Applications:

1. **Continuous bio-signal (e.g. ECG) monitoring** using 'resource constraint' wearable devices.
2. Smaller Φ enables segmented column/row-based sensing of **larger images**.



Segmentation-based Recovery

$$\underbrace{\underbrace{\mathbf{y}_{M' \times 1}} \quad \underbrace{\mathbf{y}_{M' \times 1}}}_{p \text{ smaller segments}} \quad \mathbf{y}_{M \times 1} \text{ (where } M = M' \times p \text{)} \quad \underbrace{\mathbf{y}_{M' \times 1}}$$

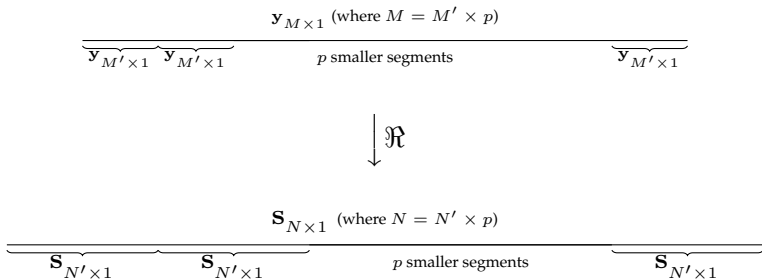


Segmentation-based Recovery

$$\begin{array}{c} \mathbf{y}_{M \times 1} \text{ (where } M = M' \times p \text{)} \\ \hline \underbrace{\mathbf{y}_{M' \times 1}} \quad \underbrace{\mathbf{y}_{M' \times 1}} \quad \dots \quad \underbrace{\mathbf{y}_{M' \times 1}} \\ p \text{ smaller segments} \\ \hline \downarrow \mathcal{R} \end{array}$$



Segmentation-based Recovery





1. Performing recovery p times \rightarrow Computationally expensive.



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2. **Degradation** in reconstruction quality caused by segmentation.



Question?

Concatenate p individual segments of \mathbf{y} \rightarrow Form $\mathbf{y}_{M \times 1}$ \rightarrow
Perform recovery once.



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$\Phi_{M' \times N'}$ constructed during measurement $\rightarrow \Phi_{M \times N}$ **can't be reconstructed!**

Solution?

$\Phi_{M' \times N'}$ can be expanded to form $\Phi_{M \times N}$.



$$\hat{\Phi}_{M \times N}$$



$$\hat{\Phi}_{M \times N} = \mathbf{I}_{p \times p} \otimes \Phi_{M' \times N'}$$



$$\hat{\Phi}_{M \times N} = \mathbf{I}_{p \times p} \otimes \Phi_{M' \times N'} = \begin{bmatrix} \Phi & \mathbf{0} & \dots & \mathbf{0} \\ \mathbf{0} & \Phi & \dots & \mathbf{0} \\ & & \ddots & \\ \mathbf{0} & \mathbf{0} & \dots & \Phi \end{bmatrix}$$



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$$\mathbf{s}_{N \times 1} = \Re(\mathbf{y}_{M \times 1}, \hat{\mathbf{\Phi}}_{M \times N}, \hat{\mathbf{\Psi}}_{N \times N})$$



Advantage

Computationally expensive recovery algorithm performs **once**,
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Advantage

Computationally expensive recovery algorithm performs **once**, not p times.

Issue

Quality degradation not addressed.



$$\Psi'_{N \times N} = \begin{bmatrix} \Psi'_{1,1} & \Psi'_{1,2} & \cdots & \Psi'_{1,p} \\ \Psi'_{2,1} & \Psi'_{2,2} & \cdots & \Psi'_{2,p} \\ & & \ddots & \\ \Psi'_{p,1} & \Psi'_{p,2} & \cdots & \Psi'_{p,p} \end{bmatrix}$$



$$\mathbf{s}_{N \times 1} = \Re(\mathbf{y}_{M \times 1}, \hat{\mathbf{\Phi}}_{M \times N}, \mathbf{\Psi}'_{N \times N})$$



$$\mathbf{s}_{N \times 1} = \Re(\mathbf{y}_{M \times 1}, \hat{\Phi}_{M \times N}, \Psi'_{N \times N})$$

Remains unchanged

Regenerated from the same basis



Theorem

Let us consider the resultant Kronecker-based sparsifying matrix $\hat{\Psi}_{N \times N} = \mathbf{I}_{p \times p} \otimes \Psi_{N' \times N'}$ is of size $N \times N$. If the modified sparsifying basis $\Psi'_{N \times N}$ is regenerated from the same basis then,

$$\mu(\hat{\Phi}_{M \times N}, \hat{\Psi}_{N \times N}) \geq \mu(\hat{\Phi}_{M \times N}, \Psi'_{N \times N})$$



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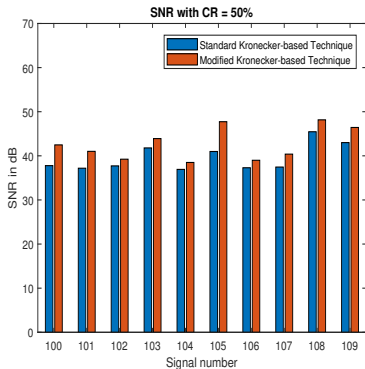
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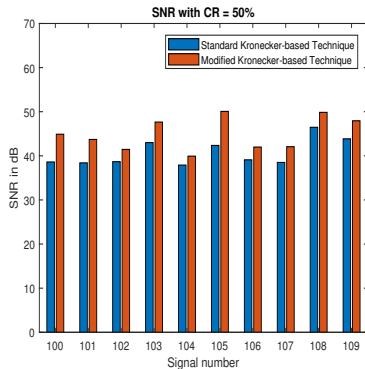
1. Reconstruction quality **improves**.
2. Recovery is performed **once, not p times**.



Kronecker CS-based 1-D Signal Recovery



(a) Reconstructed signal² with random matrix (Normal distribution) for CR = 50%



(b) Reconstructed signal with random matrix (Bernoulli distribution) for CR = 50%

²"MIT-BIH Arrhythmia Database." Available: <https://www.physionet.org/physiobank/database/mitdb/>

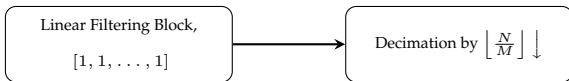


Deterministic Measurement

- To ensure **easy realisation** deterministic sensing is adopted.



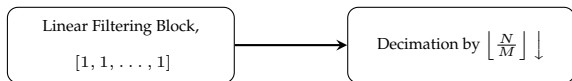
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- **Linear filtering**-based DBBD³ deterministic matrix is used in this work.



³A. Ravelomanantsoa, H. Rabah and A. Rouane, "Compressed sensing: A simple deterministic measurement matrix and a fast recovery algorithm," *IEEE Transactions on Instrumentation and Measurement*, vol. 64, pp. 3405–3413, Dec 2015



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- A matrix representation of DBBD deterministic matrix for $M = 4$ and $N = 16$.

$$\Phi_{4 \times 16} = \begin{bmatrix} [1111] & & & \\ & [1111] & & \\ & & [1111] & \\ & & & [1111] \end{bmatrix}$$

³A. Ravelomanantsoa, H. Rabah and A. Rouane, "Compressed sensing: A simple deterministic measurement matrix and a fast recovery algorithm," *IEEE Transactions on Instrumentation and Measurement*, vol. 64, pp. 3405–3413, Dec 2015



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- ✓ DBBD matrix **preserves morphology** in the compressed domain.
- ✓ Enables signal processing in the **compressed domain**.



Kronecker CS-based 1-D Signal Recovery

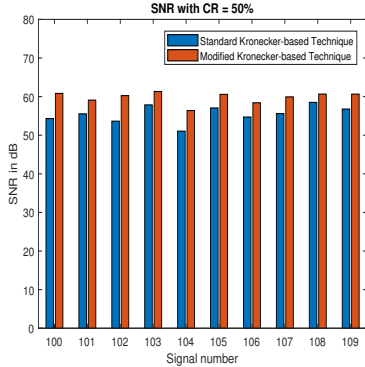


Figure: Reconstructed signal with DBBD deterministic matrix for CR = 50%



Kronecker CS-based 1-D Signal Recovery

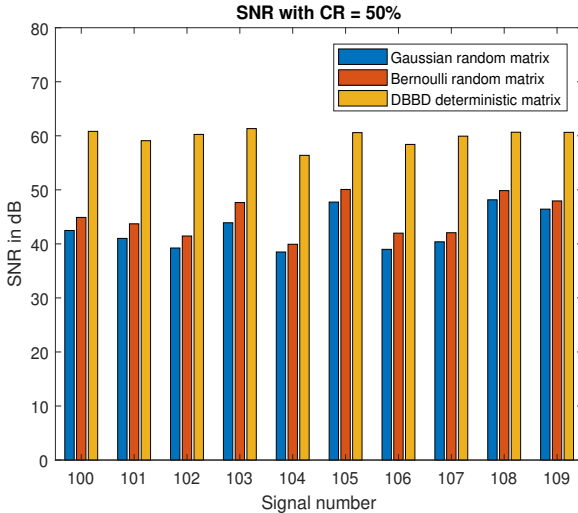


Figure: Comparison of signal quality using random and deterministic matrices for CR = 50%



Table: Statistical analysis of recovery performance using modified Kronecker-based technique: CR = 50%, Φ = DBBD

Statistical Parameter	SNR (dB)							
	Biorthogonal	Coiflets	Daubechies	DCT	Haar	Discrete Meyer	Reverse Biorthogonal	Symlets
Minimum	5.31	21.69	17.45	35.17	20.79	31.19	12.46	17.45
Maximum	26.61	23.65	26.76	35.17	20.79	31.19	27.00	36.62
Median	21.96	22.90	23.20	35.17	20.79	31.19	23.08	21.74



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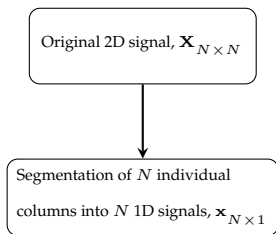


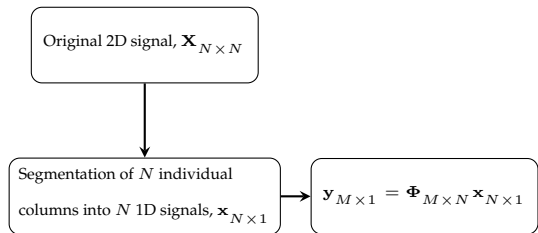
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- ✓ **DCT** serves as better Ψ for DBBD measurement matrix.
- ✓ **Filtering effect** of DBBD makes it suitable for measuring noisy signals.

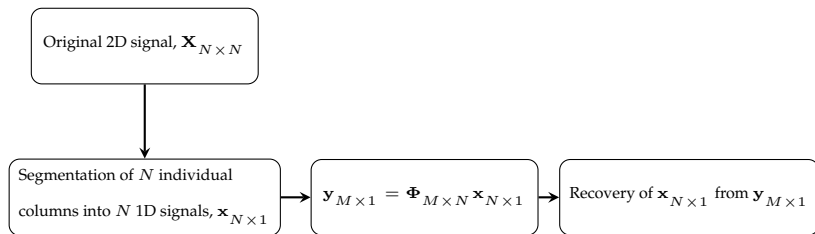
Extension to 2-D Signals

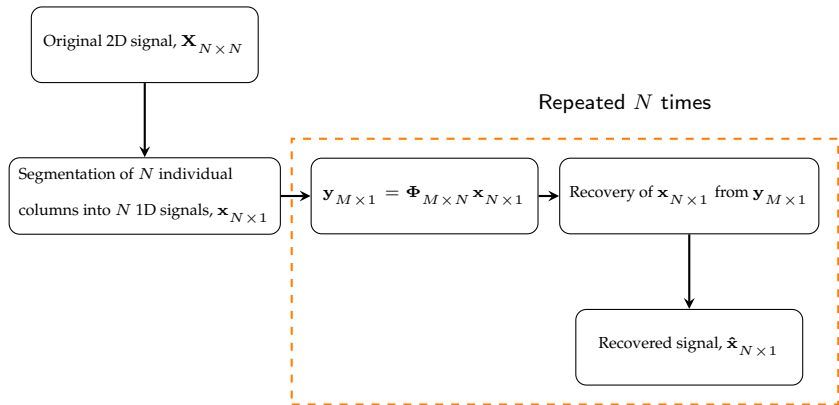


Original 2D signal, $\mathbf{X}_{N \times N}$











Column-wise Measurement

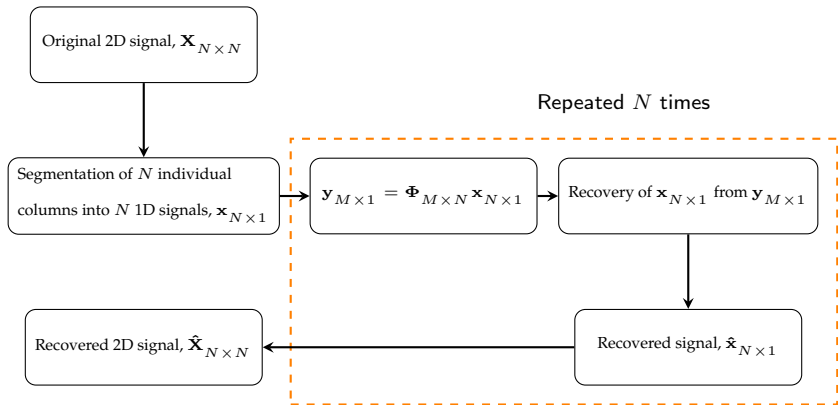




Figure: Original image ⁴



Modified Kronecker-based Recovery for 2-D Signals



(a) Reconstructed image using standard Kronecker-based technique



(b) Reconstructed image using modified Kronecker-based technique



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$X_{N \times N}$



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$Y_{M \times N}$

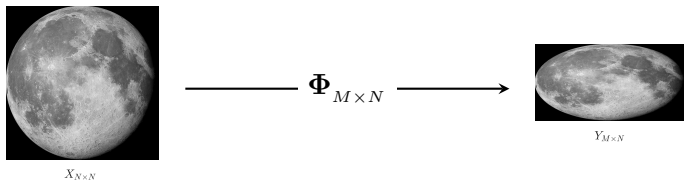


$X_{N \times N}$

$$\longrightarrow \Phi_{M \times N} \longrightarrow$$

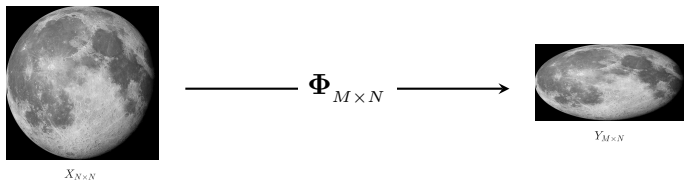


$Y_{M \times N}$



Takeaways

- ✓ **Aspect ratio** of the compressed image **not** preserved.



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- ✓ **Aspect ratio** of the compressed image **not** preserved.
- ✓ **Compressed domain** classification becomes **difficult**.
- ✓ Images stored in the compressed domain required **storage space** for an $M \times N$ matrix.



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Takeaways

- ✓ **Aspect ratio** of the compressed image **not** preserved.
- ✓ **Compressed domain** classification becomes **difficult**.
- ✓ Images stored in the compressed domain required **storage space** for an $M \times N$ matrix.
- ✓ Measurement is required to be performed **N times**.



Original 2D signal, $\mathbf{X}_{N \times N}$



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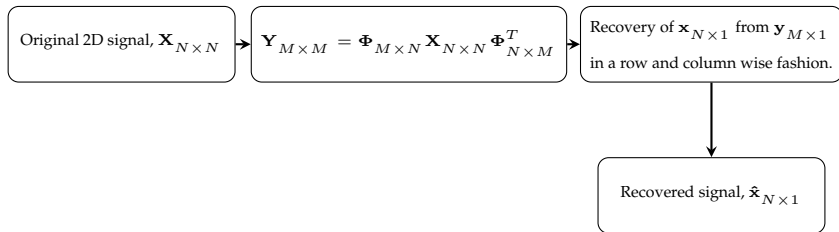
$$\rightarrow \mathbf{Y}_{M \times M} = \Phi_{M \times N} \mathbf{X}_{N \times N} \Phi_{N \times M}^T$$

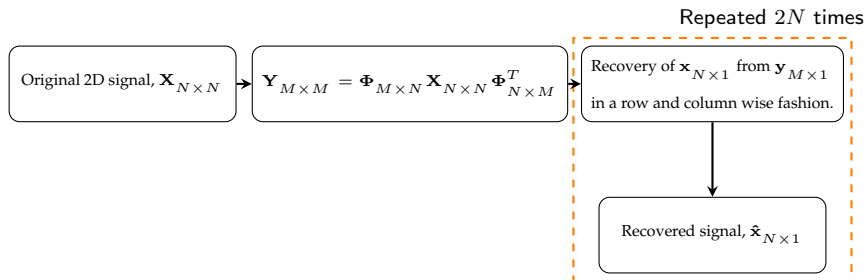


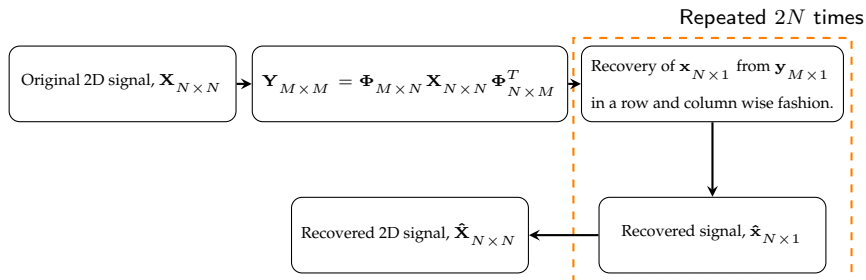
Original 2D signal, $\mathbf{X}_{N \times N}$

$$\mathbf{Y}_{M \times M} = \Phi_{M \times N} \mathbf{X}_{N \times N} \Phi_{N \times M}^T$$

Recovery of $\mathbf{x}_{N \times 1}$ from $\mathbf{y}_{M \times 1}$
in a row and column wise fashion.









$X_{N \times N}$



$X_{N \times N}$



$Y_{M \times M}$



$X_{N \times N}$

$$\longrightarrow \Phi_{M \times N} \mathbf{X}_{N \times N} \Phi_{N \times M}^T \longrightarrow$$



$Y_{M \times M}$



$X_{N \times N}$

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Takeaways

- ✓ **Aspect ratio** of the compressed image **is preserved**.



$X_{N \times N}$

$$\longrightarrow \Phi_{M \times N} \mathbf{X}_{N \times N} \Phi_{N \times M}^T \longrightarrow$$



$Y_{M \times M}$

Takeaways

- ✓ **Aspect ratio** of the compressed image **is preserved**.
- ✓ Images stored in the compressed domain requires **lesser storage** space ($M \times M$ matrix), compared to the column-wise technique.

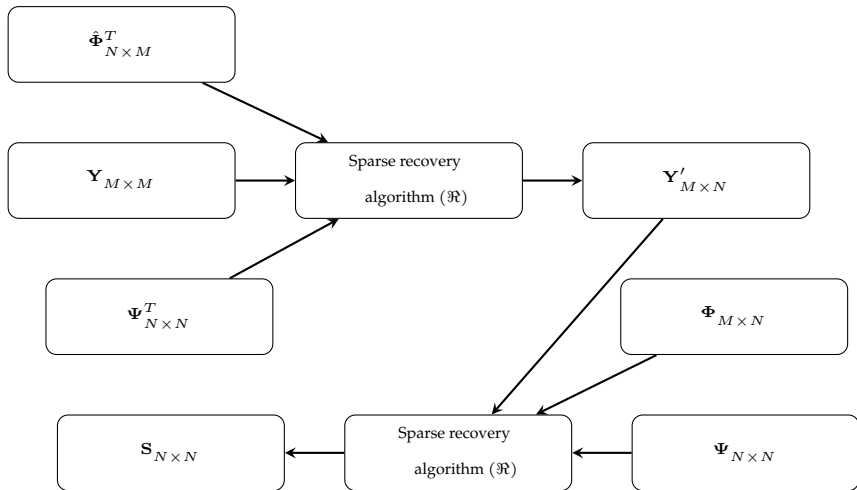


Figure: Block diagram representation of modified 2-D CS recovery.

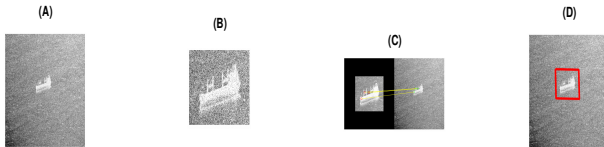


Infra-red Image (Without Noise)





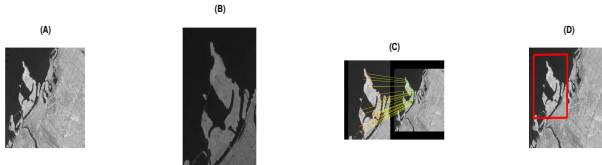
Infra-red Image (With Noise⁴)



⁴White Gaussian noise of 0 mean and variance of 0.03 has been added.

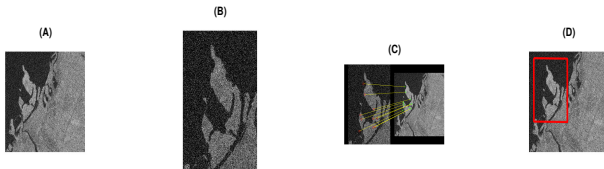


Medium Resolution Image (Without Noise)



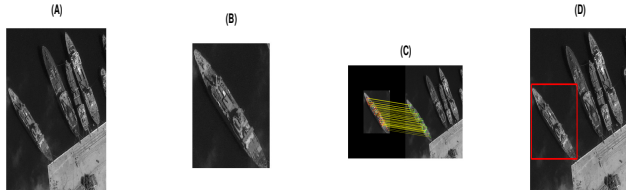


Medium Resolution Image (With Noise)



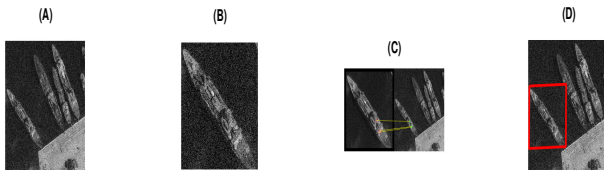


High Resolution Image (Without Noise)





High Resolution Image (With Noise)





- ✓ Development of modified Kronecker-based recovery technique for **deterministic CS** for 1-D and 2-D signals.



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- ✓ Development of modified Kronecker-based recovery technique for **deterministic CS** for 1-D and 2-D signals.
- ✓ **Comparison** of deterministic and random CS frameworks for signal quality improvement using modified Kronecker-based recovery technique.
- ✓ Development of a **novel 2-D aspect ratio preserving** CS technique and application of modified Kronecker-based recovery technique for 2-D signals.
- ✓ Demonstration of structure and morphology preservation through 2-D deterministic aspect ratio preserving CS → **Signal processing in the compressed domain without the need for any recovery.**



- ✓ Development of modified Kronecker-based recovery technique for **deterministic CS** for 1-D and 2-D signals.
- ✓ **Comparison** of deterministic and random CS frameworks for signal quality improvement using modified Kronecker-based recovery technique.
- ✓ Development of a **novel 2-D aspect ratio preserving** CS technique and application of modified Kronecker-based recovery technique for 2-D signals.
- ✓ Demonstration of structure and morphology preservation through 2-D deterministic aspect ratio preserving CS → **Signal processing in the compressed domain without the need for any recovery.**
- ✓ Investigation of Kronecker-based CS recovery technique for ECG signals using **various sparsifying dictionaries, measurement matrices and noise levels for various compression levels.**



Journal Publications

1. **D. Mitra**, H. Zanddizari and S. Rajan, "Investigation of Kronecker-based Recovery of Compressed ECG Measurements," under revision after first submission to *IEEE Transactions on Instrumentation and Measurement*, 2019.
2. H. Sadreazami, **D. Mitra**, S. Rajan and M. Bolic, "Fall Detection in Compressed Domain using Machine Learning," 2019. (Under Preparation).

Conference Publications

1. **D. Mitra**, S. Rajan and B. Balaji, "Deterministic compressive sensing approach for compressed domain image analysis," in *2019 IEEE Sensors Applications Symposium (SAS)*, France, March 2019.
2. **D. Mitra**, H. Zanddizari and S. Rajan, "Improvement of recovery in segmentation-based parallel compressive sensing," in *2018 IEEE International Symposium on Signal Processing and Information Technology (ISSPIT)*, pp. 501-506, Lousville, USA, Dec 2018.
3. **D. Mitra**, H. Zanddizari and S. Rajan, "Improvement of signal quality during recovery of compressively sensed ECG signals," in *2018 IEEE International Symposium on Medical Measurements and Applications (MeMeA)*, pp. 1-5, Rome, Italy, June 2018.



✓ Hardware-based implementation of Kronecker-based recovery and 1-D signal acquisition.



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- ✓ Possibility of Kronecker-based measurement for an extension to multi-dimensional signal processing (such as 3-D MRI).

Additional Results & Discussions

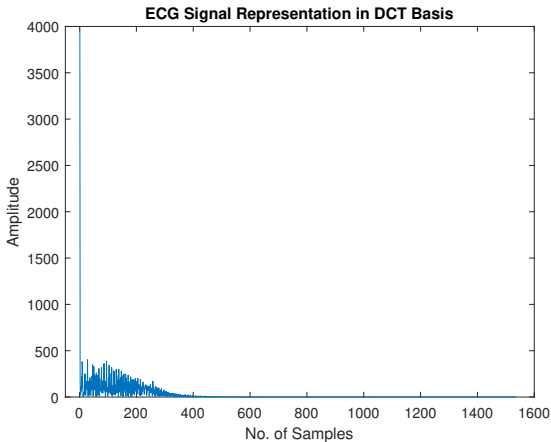


Figure: DCT domain representation of ECG signal



Selection of Φ

Random Matrix \rightarrow Gaussian or Normal, Bernoulli etc.

Deterministic matrix \rightarrow DBBD, Toeplitz-structured matrix, second-order Reed Muller code based matrix etc.



Selection of Φ

Random matrices \rightarrow



Selection of Φ

Random matrices \rightarrow

- **Difficult** to implement in hardware.



Selection of Φ

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- **Difficult** to implement in hardware.
- Encodes the measurements \rightarrow **Privacy preservation** for wireless transmission of measurements.



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Deterministic matrices \rightarrow

- **Easier** to implement in hardware.
- Morphology is **preserved** in the compressed domain.
- Reconstruction quality **improves** compared to the random matrices for a fixed Ψ .



Figure: Original Image



Column-wise Sensing and Segmentation of 2-D Signals



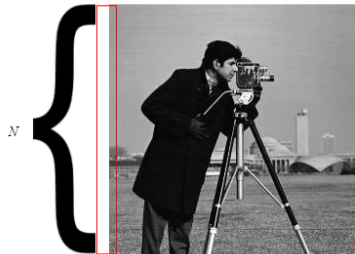


Column-wise Sensing and Segmentation of 2-D Signals





Column-wise Sensing and Segmentation of 2-D Signals



– Segmentation →





Quality Analysis for 2-D Signals

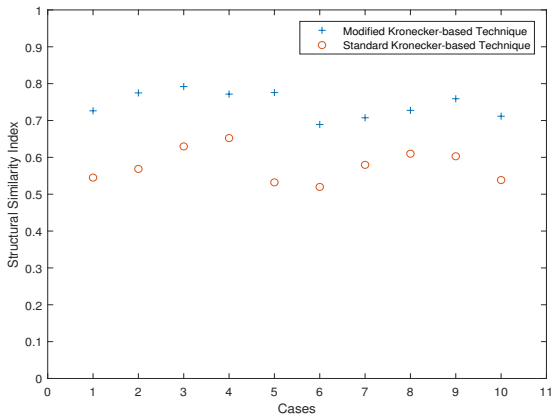


Figure: SSIM Analysis for CR = 93.75%



Quality Comparison for Segmentation

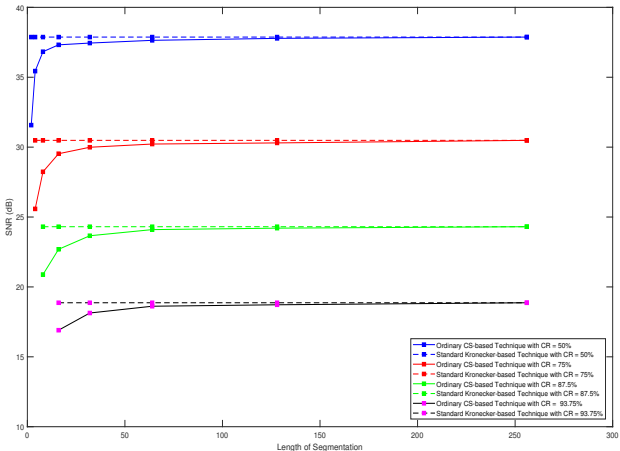


Figure: Reconstruction quality comparison between segmentation-based CS and ordinary CS methods.